INVESTOR PROTECTION, OPTIMAL INCENTIVES, AND ECONOMIC GROWTH*

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Does investor protection foster economic growth? To assess the widely held affirmative view, we introduce investor protection into a standard overlapping generations model of capital accumulation. Better investor protection implies better risk sharing. Because of entrepreneurs’ risk aversion, this results in a larger demand for capital. This is the demand effect. A second effect (the supply effect) follows from general equilibrium restrictions. Better protection (i.e., higher demand) increases the interest rate and lowers the income of entrepreneurs, decreasing current savings and next period’s supply of capital. The supply effect is stronger the tighter are the restrictions on capital flows. Our model thus predicts that the (positive) effect of investor protection on growth is stronger for countries with lower restrictions. Cross-country data provide support for this prediction, as does the detailed examination of the growth experiences of South Korea and India.

I. INTRODUCTION

Investor protection is defined by the extent to which the commercial law and its enforcement protect investors from expropriation by company insiders. A widely held view is that better investor protection, via its impact on firms’ ability to raise external financing, has a positive effect on aggregate economic growth. The acceptance of this conjecture is evidenced by the policy recommendations that the World Bank, the International Monetary

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Fund, and the European Bank for Reconstruction and Development routinely make to the countries they assist.¹

In this paper we explore the impact of investor protection on growth and welfare in a simple extension of Diamond’s [1965] overlapping generations model of capital accumulation. In our setup, each young individual has access to a decreasing returns to scale production technology. Unlike Diamond, the outcome of the production process is stochastic, i.i.d. across technologies, and known only to the technology’s owner. Lacking an initial endowment and needing resources to use their technology, young individuals, who we refer to as entrepreneurs, borrow capital from the old through financial intermediaries. These intermediaries transfer resources from the old to the young by borrowing from the old at the equilibrium rental rate and lending to the young via optimal contracts whose terms are contingent on all public information. Like much of the literature on optimal contracts with hidden information, we model the interaction between intermediaries and entrepreneurs as a message game.

We assume that it is costly for entrepreneurs to misreport outcomes and conceal resources. A fraction of any hidden resources is lost. If hiding is costless, there is no investor protection. If hiding is so difficult that all hidden resources are lost, investor protection is perfect. Our hiding cost resembles Lacker and Weinberg’s [1989] falsification cost and is intended to capture all the institutional features that limit the ability of insiders to expropriate outside investors.

The degree of risk sharing implied by the optimal contract is monotone in the level of investor protection: the better the protection; i.e., the larger the cost of hiding resources, the lower the risk borne by borrowers. Thus, better investor protection leads to better risk sharing. Our main result is that the relation between investor protection and growth depends on two opposing effects. The first, the demand effect, supports a positive association between investor protection and growth. An improvement in investor protection leads to better risk sharing. As in any partial-equilibrium model of investment with risk-averse entrepreneurs, better risk sharing implies a larger demand for capital at any given interest rate. The second, the supply effect, is a general equilibrium effect that suggests a negative association between

¹. Several of these recommendations are inspired by the OECD corporate governance standards and guidelines, discussed in OECD [1999].
investor protection and growth. For a given aggregate capital stock, better investor protection (i.e., a higher demand schedule) implies a higher interest rate, which, given the total resources available, translates into lower income for entrepreneurs. In other words, an improvement in investor protection prompts a redistribution away from entrepreneurs (the young generation) and toward lenders (the old generation). As a result, current savings and the supply of capital in the following period decrease.

The strength of the supply effect, and therefore the sign of the net effect of investor protection on growth, depends on international capital mobility. The supply effect is most powerful in a closed economy. In that case, better investor protection may even lead to a lower growth rate and smaller steady state capital and output. At the other extreme, in a small economy without restrictions on capital flows, the interest rate is fixed by world capital markets. Thus, the supply effect disappears. Better investor protection invariably implies higher growth rates and greater steady state levels of capital and output. These two extreme cases are unlikely to be descriptive of any national economy. In the data, both demand and supply effects will typically be at work, with the supply effect being stronger the more capital flows are restricted. It follows that the positive effect of investor protection on growth should be larger for countries that impose fewer restrictions on capital flows.

Do cross-country data provide any support for our predictions? We address this question in three ways. First, we explore the relation between investor protection and risk sharing. We cannot measure risk sharing directly. However, it can be argued that when entrepreneurs are better able to share risk, debt should account for a smaller fraction of external finance and ownership concentration should be lower. We show that countries characterized by better protection (as measured by the indicators introduced by La Porta, Lopez-de-Silanes, Shleifer, and Vishny [1998]), display lower ratios of debt to total external finance and less concentrated ownership. We interpret this evidence as empirical support for our model’s prediction of a positive correlation between investor protection and risk sharing. Second, we employ standard techniques from the empirical growth literature to investigate the nature of the relation between investor protection and growth. Consistent with earlier studies, we find a positive association. A novel finding is that, consistent with our theoretical analysis, investor protection has a much greater impact on
growth in more open economies. Finally, we consider in detail the development experiences of South Korea and India. In the post-World War II period, similar growth-promoting policies resulted in a much higher saving rate and growth rate in South Korea than in India. According to La Porta, Lopez-de-Silanes, Shleifer, and Vishny [1998], Indian investors have enjoyed better protection than their Korean counterparts. Since both countries have severely restricted international capital flows for most of the period under consideration, the outcome just described is exactly what our model would have predicted. According to our theoretical analysis, in Korea the low level of protection led to a redistribution of resources toward the entrepreneurial sector. Since entrepreneurs have a higher propensity to save, this led to higher capital accumulation and faster growth.

A key component of our model is the decision problem of a risk-averse entrepreneur acquiring capital from perfectly diversified investors, in an environment characterized by imperfect investor protection. Others have studied variations on this problem. The work of Himmelberg, Hubbard, and Love [2002] and Himmelberg and Quadrini [2002] is the closest to ours. As is the case here, their analysis implies that imperfect investor protection, via its effect on risk sharing, induces a suboptimal firm size. However, since their work is in partial equilibrium, it cannot tell us whether a change in investor protection triggers a redistribution of resources across agents, or to what extent such redistribution affects aggregates' dynamics. In order to address these questions, a general equilibrium analysis is required. To our knowledge, Shleifer and Wolfenzon [2002] were the first to imbed a model of corporate finance similar to the one described above in a general equilibrium framework. Their analysis has three shortcomings: entrepreneurs are assumed to be risk-neutral; agents are constrained to suboptimal financing contracts; and the model is static. Instead, we study a dynamic model in which risk-averse entrepreneurs sign constrained Pareto-optimal contracts.

Our paper also contributes to the large literature on the relation between capital accumulation and imperfections in financial markets. In particular, we have in mind the class of general equilibrium heterogeneous agents models that build on Aiyagari [1994]. In Aiyagari's case, precautionary savings imply a positive effect of imperfect risk sharing on capital accumulation. Our framework differs along several dimensions. Most important, in our scenario, since second-period income is known to agents
when they make their saving decision, there is no precautionary motive. Another difference is that, in our model, the degree of market incompleteness is endogenous: suboptimal risk sharing is induced by asymmetric information. This is also a feature of Marcet and Marimon [1992] and Khan and Ravikumar [2001]. However, our model’s prediction for the relation between market incompleteness and growth is very different from theirs. In Marcet and Marimon [1992] imperfect risk sharing has no effect on capital accumulation. According to Khan and Ravikumar [2001], an economy with private information and partial insurance displays lower growth rates of capital and output than an economy with symmetric information and full insurance. In subsection III.B we explain the basic differences among their frameworks and ours. Finally, our work is also related to the seminal studies of the relationship between financial market development and growth, e.g., Greenwood and Jovanovic [1990] and Bencivenga and Smith [1991].

The remainder of the paper is organized as follows. The model is introduced in Section II. Section III characterizes the competitive equilibrium allocation in a closed economy and identifies the demand and supply effects. In Section IV we explore the small open economy case. In Section V we derive the empirical implication for the relation between investor protection, capital mobility, and growth, and we conduct the data analysis. Section VI concludes.

II. Model

We consider a simple extension of the standard two-period Overlapping Generations Model.² The population is constant, and the measure of each cohort is normalized to one. Individuals are risk-averse. Preferences are time-separable, and the period utility, denoted by $u(c_t)$, displays constant relative risk aversion.³ Let $\sigma$ denote the coefficient of relative risk aversion. Agents discount second-period utility at the rate $\beta; \beta > 0$.

Young individuals, the entrepreneurs, are endowed with investment opportunities described by the technology $F(z_t, k_t) = \ldots$
$z_t f(k_t)$, where $k$ denotes physical capital. We assume that $f$ is $C^2$ and satisfies $f(0) = 0$, $f' > 0$, $f'' < 0$, $\lim_{k \to 0} f'(k) = \infty$, and $\lim_{k \to \infty} f'(k) = 0$. Capital depreciates at the constant rate $\delta \in (0,1)$. The random variable $z_t$ determines the quality of the investment project. We assume that for every $t$, $z_t \in \{z_i, z_h\}$, where $z_h > z_i$ and $pr(z_t = z_h) = \rho; \rho \in (0,1)$.

Old individuals do not work, and consume from assets accumulated when young. Since entrepreneurs have no endowment, they can undertake their projects only if the old generation finances them. We assume financial intermediaries that borrow capital from the old cohort at the equilibrium rental rate, and lend to entrepreneurs via Constrained-Pareto optimal one-period contracts. In Appendix 1 we discuss why we focus on one-period contracts. The intermediation sector is perfectly competitive with free entry.

The realization of the random variable $z_t$ is private information for the entrepreneurs, who have the option of hiding some of their cash flows from their financiers. Hiding, however, is costly. For every unit of cash flow hidden, an entrepreneur ends up with only the fraction $\xi \in [0,1]$. The balance is lost in the hiding process. The parameter $\xi$ is our measure of investor protection—the larger is $\xi$, the lower the protection. The two extreme values identify the cases of complete absence of protection ($\xi = 1$) and perfect protection ($\xi = 0$).

Figure I displays the timing. At the outset, an entrepreneur borrows capital $k_t$ from an intermediary, then invests and produces output equal to $z_t f(k_t)$. Next, he makes a claim about the quality of his project $\hat{z}_t \in \{z_h, z_i\}$, gives the intermediary output consistent with this claim, i.e., $\hat{z}_t f(k_t)$, and receives a contingent transfer $\tau_{ht}$. Therefore, a financing contract consists of a capital advance $k_t$ and contingent transfers $\tau_{ht}$ and $\tau_{lt}$.

At the end of the first period, entrepreneurs end up with income we denote by $m_t$. If the project is of low quality, $m_t = \tau_{lt}$. Having no endowment, an agent is unable to misreport in the low

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4. It is straightforward to modify our setup to allow for balanced growth, provided that the technology is consistent with it (e.g., with Cobb-Douglas). It suffices to assume that $z_{i,t+1}/z_{i,t} = \gamma > 1$ for $i = h,l$. All of our results would hold for the modified model, once variables were detrended.

5. All of our results follow even when some or all of this balance accrues to the intermediaries. The only caveat is that it is necessary to work with a continuum of outcomes. Otherwise, any hiding would be detected by the lender. See Appendix 2 for details.

6. In Appendix 2 we show that the Constrained-Pareto optimal contract always requires the output surrendered to be consistent with the report. In turn, this implies no hiding along the equilibrium path.
state, since that would entail surrendering a level of output $zhf(kt)$. If the project is of high quality, truthful reporting yields $mt = \tau_{ht}$, and concealing yields $mt = \tau_{lt} + \xi\Delta f(k_t)$, where $\Delta = zh - z_l$. By misreporting, the entrepreneur receives the transfer intended for low quality projects, $\tau_{lt}$, plus the fraction $\xi$ of the hidden output $\Delta f(k_t)$. At the end of the period, agents consume part of their income and save the rest. At the beginning of the second stage, they lend their savings to intermediaries at the market rate, and intermediaries lend those funds to the new cohort of young people. At the end of their lives, agents receive and consume principal and interest.

### III. Competitive Equilibrium

Consider an entrepreneur’s consumption-saving decision. Let $v(m_t, r_{t+1})$ denote the indirect utility of an agent born at time $t$, conditional on having received an income $m_t$ and on facing an interest rate $r_{t+1}$. Then,

$$v(m_t, r_{t+1}) = u[m_t - s(m_t, r_{t+1})] + \beta u[(1 + r_{t+1})s(m_t, r_{t+1})],$$

where the optimal saving function $s(m_t, r_{t+1})$ is

$$s(m_t, r_{t+1}) = \arg \max_s \{u(m_t - s) + \beta u[(1 + r_{t+1})s]\}. (1)$$
An optimal contract is a triple \((k_t, \tau_{ht}, \tau_{lt})\) that solves the optimization problem:

\[
\begin{align*}
(P2) \quad & \max_{k_t, \tau_{ht}, \tau_{lt}} \rho v(\tau_{ht}, r_{t+1}) + (1 - \rho) v(\tau_{lt}, r_{t+1}), \\
& \text{subject to incentive compatibility for entrepreneurs whose projects are high quality,} \\
& (2) \quad v(\tau_{ht}, r_{t+1}) \geq v[\tau_{lt} + \xi \Delta f(k_t), r_{t+1}], \\
& \text{and the zero-profit condition for intermediaries,} \\
& (3) \quad \tilde{\tau}_t \equiv \rho \tau_{ht} + (1 - \rho) \tau_{lt} = \tilde{z} f(k_t) - (r_t + \delta) k_t,
\end{align*}
\]

where \(\tilde{z} \equiv \rho z_h + (1 - \rho) z_l\). We now define a competitive equilibrium.\footnote{Since every generation consists of a measure one of ex ante identical individuals, the capital assigned to every entrepreneur must equal aggregate capital. For this reason, we use the same notation for the two variables.}

**DEFINITION.** Given an initial capital stock \(k_0 > 0\), a competitive equilibrium is a consumption level of the initial old \(c_0^o\), contingent consumption allocations for young and old individuals, \({c^y_{ht}, c^y_{lt}}\}_{t=0}^\infty\) and \({c^o_{ht}, c^o_{lt}}\)\(_{t=0}^\infty\), and sequences of contracts, \({k_t, \tau_{ht}, \tau_{lt}}\)\(_{t=0}^\infty\), and interest rates, \({r_t}\)\(_{t=0}^\infty\), such that

1. consumers optimize, i.e., \(c^o_0 = k_0 (1 + r_0)\), and for \(i = h, l\) and \(t \geq 0\), \(c^y_{it} = \tau_{it} - s(\tau_{it}, r_{t+1})\) and \(c^o_{it+1} = s(\tau_{it}, r_{t+1})(1 + r_{t+1})\);
2. contracts are optimal, i.e., for all \(t \geq 0\), they solve problem (P1); and
3. the goods market clears at all \(t \geq 0\):

\[
(4) \quad k_{t+1} = \rho s(\tau_{ht}, r_{t+1}) + (1 - \rho) s(\tau_{lt}, r_{t+1}).
\]

In the remainder of this section we characterize the evolution of this economy, and then explore how the nature of financial claims and the paths of variables such as capital and output change in response to variations in the investor protection parameter \(\xi\).

**III.A. Benchmark: Perfect Investor Protection (\(\xi = 0\))**

For \(\xi = 0\), our model is effectively Diamond’s [1965]. Thus, for every \(t\), given an interest rate \(r_t\), the demand for capital satisfies the optimality condition
Also, strict concavity of the utility function implies that $\tau_{ht} = \tau_{lt}$. Since intermediaries are risk-neutral, an optimal contract insures entrepreneurs fully, making intermediaries residual claimants on the projects’ cash flows. From the zero-profit condition, together with (5), transfers are functions of capital only, and are given by

$$\tau_t = \tau(k_t) = \tilde{z}[ f(k_t) - f'(k_t)k_t].$$

The gross return on investment for the intermediaries $R_{it}$ is given by

$$R_{it} = (z_i f(k_t) - \tau_t)/k_t \text{ for } i = h, l,$$

and it follows that

$$R_{ht} - R_{lt} = \Delta f(k_t)/k_t.$$

The financial claims held by the intermediaries resemble equity claims. Finally, given $k_0 > 0$, the behavior of the economy is completely described by (5), along with the difference equation

$$k_{t+1} = s[\tau(k_t), r_{t+1}].$$

For $\xi = 0$, our economy evolves exactly as a standard OLG model with constant productivity $\tilde{z}$, competitive capital and labor markets, and inelastic labor supply; the wage is equal to $\tau_t$.

### III.B. Imperfect Investor Protection ($\xi \in (0,1)$)

In this subsection we show that when $\xi > 0$, the effect of investor protection on capital accumulation can be decomposed into a (positive) demand effect and a (negative) general equilibrium effect on supply. While the net effect ultimately depends on the utility specification, it turns out that for a large subset of the parameter space better investor protection leads to less investment and less accumulation. The intuition is as follows. Lower $\xi$ (better investor protection) implies better risk sharing. This means that entrepreneurs will demand more capital for a given interest rate. This is the demand effect. For given capital, however, lower risk will demand a lower expected return. That is, the average level of transfers from intermediaries to entrepreneurs will be lower. This implies that on average entrepreneurs will
earn less and save less, so that the capital supply curve will also be lower. This is the supply effect. In the remainder of this subsection, we characterize the demand effect, and we show how it interacts with the supply effect.

To begin, observe that for any \( r_t + 1 \), \( v(\tau_t, r_{t+1}) \) is strictly increasing and strictly concave in \( \tau_t \). By strict concavity, (2) must bind in the solution. Then, by strict monotonicity, it follows that \( \tau_{ht} = \tau_{lt} + \frac{\xi \Delta f(k_t)}{k_t} \) for any \( t \). Using the zero-profit condition (3), transfers are

\[
\tau_{lt} = \tau_l(k_t, r_t) = (\tilde{z} - \rho \xi \Delta) f(k_t) - (r_t + \delta) k_t
\]

and

\[
\tau_{ht} = \tau_h(k_t, r_t) = (\tilde{z} + (1 - \rho) \xi \Delta) f(k_t) - (r_t + \delta) k_t.
\]

Substituting for \( \tau_{lt} \) and \( \tau_{ht} \) in (6) yields

\[
R_{ht} - R_{lt} = \frac{(1 - \xi) \Delta f(k_t)}{k_t}.
\]

Risk sharing is imperfect. Since \( (R_{ht} - R_{lt}) k_t < \Delta f(k_t) \), entrepreneurs bear part of the risk. Also, this part is increasing in \( \xi \). In the extreme, when \( \xi = 1 \), the contract provides no risk sharing at all, and the claim held by the intermediary amounts to a standard debt contract.

Next, the aggregate demand for capital is decreasing in both \( r_t \) and \( \xi \). To see this, observe that using the incentive compatibility condition, and letting \( y_{t+1} = f(k_t) \), problem (P1) can be restated as

\[
\max_{\tilde{y}_{t+1}} V(\tilde{t}_t, y_{t+1}) = \rho v[\tilde{t}_t + (1 - \rho)\Delta \xi y_{t+1}] + (1 - \rho) v[\tilde{t}_t - \rho \Delta \xi y_{t+1}] - (r_t + \delta) f^{-1}(y_t)
\]

subject to

\[
(BC) \quad \tilde{t}_t = \tilde{y}_t - (r_t + \delta) f^{-1}(y_t).
\]

\( V(\tilde{t}_t, y_t) \) implies a collection of level sets. The necessary conditions associated with problem (P1) can be expressed in terms of tangency between these level sets and (BC). For given \( r_t \) and \( r_{t+1} \), the optimal pair \( (\tilde{t}_t, y_t) \) must solve the system of equations given by the budget constraint (BC) and the condition

\[
(9) \quad \frac{\partial \tilde{t}_t}{\partial y_t} \bigg|_{BC} = \frac{\partial \tilde{t}_t}{\partial y_t} \bigg|_V.
\]

Using the envelope theorem,
\[
\frac{\partial \tau_t}{\partial y_t} \bigg|_{BC} = z - (r_t + \delta) \frac{df^{-1}(y_t)}{dy_t},
\]
\[
\frac{\partial \tau_t}{\partial y_t} \bigg|_v = -\rho(1 - \rho)\xi \Delta \frac{u'(c_{hl}) - u'(c_{ht})}{\rho u'(c_{hl}) + (1 - \rho)u'(c_{ht})} > 0.
\]

Since \(f\) and \(u\) are strictly concave, the level sets for \(V(\tau_t, y_t)\) are strictly convex, and the budget constraint is strictly concave. It follows that the optimal pair \((\tau_t, y_t)\) is unique. Furthermore, since the budget constraint is steeper at \(y_t = 0, \tau_t y_t > 0\). Since \(f\) is strictly increasing, the optimal \(y_t\) uniquely determines an optimal \(k_t = f^{-1}(y_t)\). The consumption allocations are then given by

\[c_{it} = \tau_i(k_t) - s(\tau_i(k_t), r_{t+1})\text{ for } i = h, l.\]

Under our assumptions on preferences, it follows that

\[c_{it} = [1 - \kappa(r_{t+1})]\tau_{it}\text{ for } i = h, l,\]

where

\[\kappa(r_{t+1}) = \frac{1}{1 + \beta^{-1} \sigma(1 + r_{t+1})^{\alpha - 1} \sigma}.\]

Finally, since the indirect utility function is log-separable in \(r_{t+1}\), we can rewrite the slope of the indifference curves as

\[
\frac{\partial \tau_t}{\partial y_t} \bigg|_V = -\rho(1 - \rho)\xi \Delta \frac{u'(\tau_{ht}) - u'(\tau_{tt})}{\rho u'(\tau_{ht}) + (1 - \rho)u'(\tau_{tt})} > 0.
\]

In turn, this implies that the optimal pair \((k_t, \tau_t)\) (and the aggregate demand for capital) does not depend on \(r_{t+1}\).

For given \(k_0 > 0\), the economy’s evolution is completely characterized by conditions (9) and (BC), which define the demand for capital \(k_t = D(r_t, \xi)\), together with (4), which defines the supply of capital \(k_{t+1} = S(k_t, r_t, r_{t+1})\).

**Proposition 1.** The function \(D(r_t, \xi)\) is strictly decreasing in both \(r_t\) and \(\xi\).

*Proof of Proposition 1.* 1. \(D(r_t, \xi)\) is decreasing in \(r_t\). Refer to Figure II. Start with an optimal \(k_0^0\). This implies that \(y_0^0 = f(k_0^0)\) and a level of the interest rate \(r_0^0 = D^{-1}(k_0^0, \xi)\). Now consider any \(r_1^0 > r_0^0\). Since \(\partial \tau_t / \partial r_t \big|_{BC} = -k_t < 0\), the budget constraint shifts from \(BC_0\) to \(BC_1\). To show that the optimal capital advance...
associated with the higher interest rate is \( k_t^1 < k_t^0 \), it is enough to show that \( \partial / \partial \tau_t (\partial \tau_t / \partial y_t) \leq 0 \). Simple calculations reveal that

\[
\frac{\partial}{\partial \tau_t} \left( \frac{\partial \tau_t}{\partial y_t} \right) = -\frac{\rho (1 - \rho) \xi \Delta u'(\tau_{ht}) u'(\tau_{ht})}{[\rho u'(\tau_{ht}) + (1 - \rho) u''(\tau_{ht})]^2} [R_A(\tau_{ht}) - R_A(\tau_{ht})],
\]

where \( R_A(\tau_{ht}) = -u''(\tau_{ht}) u'(\tau_{ht}) \) denotes the coefficient of absolute risk aversion. Therefore, a sufficient condition for \( \partial / \partial \tau_t (\partial \tau_t / \partial y_t) \leq 0 \) is that the utility function displays nonincreasing absolute risk aversion. This condition is satisfied by CRRA preferences.

2. \( D(r_t; \xi) \) is strictly decreasing in \( \xi \). Refer to Figure III. Consider any \( \xi = \xi_0 \in (0,1) \). Let \( k_t^0 \) denote the corresponding optimal capital advance, and let \( y_t^0 = f(k_t^0) \). Now consider any \( \xi_1 > \xi_0 \). The budget constraint BC is invariant to such modification. On the other hand, some algebra shows that risk aversion implies that \( \partial / \partial \xi (\partial \tau_t / \partial y_t) > 0 \). For given \( r_t \), the new optimal capital advance \( k_t^1 \) must be strictly lower than \( k_t^0 \). QED

We now turn to comparing the dynamics of two economies differing only in terms of \( \xi \). Let \( \xi \) and \( \hat{\xi} \) be the degrees of investor protection in the two economies, and suppose that \( \hat{\xi} > \xi \). Start
with $t = 0$. Since the capital stock is given, the supply of capital by the old generation is completely inelastic at $k_0$. The difference in investor protection is reflected in different demand schedules. The result, illustrated in Figure IV, is that in the economy with poorer investor protection the interest rate $r_0$ is lower and the expected income of entrepreneurs $\bar{\tau}_0$ is higher. The intuition is straightforward. Since the number of entrepreneurs is constant, the capital per entrepreneur must be $k_0$ in both economies. In the economy with poorer investor protection, the optimal contract allows for less risk sharing. For the young to accept the greater risk, their expected return $\bar{\tau}_0$ must be larger. Finally, the aggregate resource constraint dictates that this can happen only if $r_0$ is lower.

From Proposition 1, at any $t$ the demand schedule will be lower the higher the parameter $\xi$. A larger value of $\bar{\tau}_0$ implies an outward shift of the supply curve at $t = 1$. This results in a higher or lower value of $k_1$ depending on the relative slopes of demand and supply, as well as on the magnitudes of their shifts.

If the income effect deriving from an interest rate change dominates the substitution effect in a way that causes the slope of the supply curve to be greater than the slope of the demand curve
(in absolute value), then, for all \( t \geq 1 \), \( k_t(\xi) < k_t(\hat{\xi}) \). This occurs, for example, if the utility function is logarithmic. In such cases, the income and substitution effects exactly offset each other. As a result, savings are a constant proportion of transfers. This implies that at all \( t \) the supply of capital is inelastic and given by

\[
k_{t+1} = \frac{\beta}{1 + \beta} \tilde{\tau}_t.
\]

Finally, this means that for any pair \((\xi, \hat{\xi})\) with \( \hat{\xi} > \xi \), \( \tilde{\tau}_0(\hat{\xi}) > \tilde{\tau}_0(\xi) \). It will also be the case that \( k_1(\hat{\xi}) > k_1(\xi) \) and \( r_1(\hat{\xi}) < r_1(\xi) \), and thus \( \tilde{\tau}_1(\hat{\xi}) > \tilde{\tau}_1(\xi) \); refer to Figure V. By repeating the same argument at any time \( t \), we conclude that capital accumulation is always higher in the economy with poorer investor protection. 8

III.C. The Cobb-Douglas Production Function

Proposition 2 shows that when the technology is described by a Cobb-Douglas production function, entrepreneurs’ income can be expressed in a very convenient form.

8. Notice that, there being no uncertainty in the second stage of people’s lives, the precautionary motive for saving is absent in our model. Introducing such motive would reinforce the supply effect.
PROPOSITION 2. If \( f(kt) \) with \( (0,1) \), then \( \tau_{it} = g_{it}(kt) \) for some constants \( g_i, i = h, l \).

Proof of Proposition 2. Since the optimal contract \( (\tilde{\tau},k_t) \) is unique for given \( r_t \), it suffices to check that \( \tau_{it} = g_{it}(kt) \) satisfies the necessary conditions (7), (8), and (9). Therefore, assume that \( \tau_{it} = g_{it}(kt) \). Then, (9) implies that

\[
(r_t + \delta)k_t = \alpha \left[ \bar{z} + \rho (1 - \rho) \xi \Delta \frac{u'(g_h) - u'(g_i)}{\rho u'(g_h) + (1 - \rho) u'(g_i)} \right] k_i^\alpha.
\]

Substituting this expression in (7) and (8) verifies our conjecture.

The paths for capital stock and interest rate are jointly determined by the contemporaneous equation (10), which determines the demand for capital as a function of the interest rate, and by the first-order difference equation

\[
k_{t+1} = \kappa (r_{t+1}) [\rho g_h + (1 - \rho) g_i] k_i^\alpha,
\]

which defines the supply of capital.

Assessing the effect of investor protection on capital accumulation with generality is nontrivial. As argued above, the net
effect deriving from a change in investor protection depends on the relative slopes of demand and supply. Equations (10) and (11) reveal that both slopes are nonlinear in the same set of parameters. The coefficient of relative risk aversion \( \sigma \) plays a particularly important role. Clearly, it affects the magnitude of the demand shift induced by a higher \( \xi \). Since \( \sigma \) is just the inverse of the intertemporal elasticity of substitution, it also affects the shift of the supply schedule, as well as its elasticity with respect to the interest rate.

Assuming logarithmic utility removes any ambiguity. In this case, \( \kappa(r_{t+1}) = \beta/(1 + \beta) \), so the path of capital is uniquely determined by (11). Condition (10) only determines the level of the equilibrium interest rate. Since the term in square brackets in (11) is strictly increasing in \( \xi \), poorer investor protection always implies greater capital accumulation.

Even when \( \sigma \neq 1 \), our result still holds in most instances. That is, for most parameterizations, a higher value for \( \xi \) (poorer investor protection) implies higher levels of capital at all dates. When this occurs, poorer investor protection also implies higher paths for the growth rate of output and the saving rate, and a lower path for the interest rate. Figure VI shows the typical dynamics of capital, output growth rate, interest rate, entrepreneurial income, saving rate, and welfare, in a scenario with \( \sigma \neq 1 \).

Notice that the transition paths for capital depicted in Figure VI could have been generated by economies having the same level of investor protection but different levels of total factor productivity \( \tilde{\tilde{z}} \). However, according to our model, differences in TFP have very different implications for the behavior of the real interest rate. Contrary to what is implied by a lower level of investor protection, a higher level of TFP yields a uniformly higher path for the interest rate.

9. In the panel dedicated to the transfers, the top two paths depict the evolution of \( \tau_{ht} \) for two different levels of \( \xi \), the middle two paths depict the evolution of \( \tau_{it} \), and the bottom two the evolution of \( \tau_{lt} \). The levels of \( \xi \) used to produce the figure are 0.2 and 0.8, respectively. The other parameter values are \( \alpha = \frac{1}{5} \), \( \delta = 0.15 \), \( \bar{z}_h = 2 \), \( \bar{z} = 1 \), \( \rho = 0.4 \), \( \beta = 0.99 \), and \( \sigma = 0.6 \). There are parameterizations for which a higher \( \xi \) leads to lower accumulation. The demand effect tends to dominate when the discount rate \( \beta \) is low, so that the propensity to save is also low. For instance, this is the case when \( \beta = 0.2 \), with all remaining parameter values as above.

10. In our model, the real interest rate reflects not only the marginal productivity of capital, but also the degree of risk sharing in the economy. Equation (10) implies that \( r_t \) equals the marginal product, \( \alpha \bar{z} k_t^{\gamma -1} \), plus a negative term
In the example in Figure VI, the welfare of all generations is higher when investor protection is better. But this result is not general. At date $t = 0$, better investor protection always yields a higher interest rate, so that the old are better off. The welfare of the remaining generations can be increased or decreased by better investor protection, depending on the net effect of three factors, of which two are positive and one is negative. A lower $\xi$ is which depends on the level of investor protection. Entrepreneurs must be compensated for the risk induced by poor protection. This entails a lower real interest rate.
beneficial because it is associated with better risk sharing. But it also induces an increase in the rental rate at all dates, thus lowering every generation’s income in the first period (since higher rates mean lower average transfers) and raising it in the second. The net effect is negative for high enough values of the parameter $\alpha$.\textsuperscript{11}

III.D. Interpretation of the Results

The result that for closed economies poorer investor protection is generally associated with higher growth is due to the fact that lowering the level of protection induces a transfer of resources away from the old and toward the young. As argued above, lowering the level of protection has an adverse impact on the risk-sharing possibilities of entrepreneurs. This implies that for given project size, the entrepreneurs themselves will require a higher expected return. The intergenerational redistribution reflects the extent to which such a shift in the demand for capital leads to higher entrepreneurial income. In fact, in general equilibrium, for the young generation to receive more, the old must suffer an income loss. Finally, the positive impact on savings follows from the fact that young individuals have a higher propensity to save.\textsuperscript{12}

The simple demographic structure of our model implies a perfect coincidence between young and entrepreneurs, and between old and financiers. So it is obvious why entrepreneurs have higher saving rates. It should be clear, however, that the scope of our result goes beyond this simple structure. In fact, it has been argued by many that entrepreneurs tend to have higher saving rates than the rest of the population.\textsuperscript{13} As long as worsening investor protection induces a redistribution from individuals with low marginal propensities to save (outside investors) to individuals with high propensities (entrepreneurs), the correlation between investor protection and growth is more subtle and complex.

\textsuperscript{11} An example in which the welfare of future generations increases with $\xi$ is when all parameters are as in footnote 9, except for $\alpha$, that is set equal to 0.6.

\textsuperscript{12} The result that in an OLG model intergenerational redistribution might lead to higher savings is neither novel, nor specific to our environment. Under some conditions, in the familiar Diamond model, a tax on capital income whose proceeds are redistributed to the young also leads to faster capital accumulation. However, the implications for other endogenous quantities such as interest rate and welfare, are radically different. We thank an anonymous referee for making this observation. The novelty of our contribution lies in the mechanism that triggers the redistribution.

\textsuperscript{13} For example, see Gentry and Hubbard [2000].
than might be expected based on a partial-equilibrium model of investment. The reason, again, is that a worsening of investor protection redistributes resources in a way that has a positive effect on the supply of capital.

III.E. Robustness of the Results: An Assessment

A particular feature of our model is that the fraction of entrepreneurs in the economy is fixed. All projects are financed at all times, regardless of the level of investor protection. This may matter. One can think of simple variations of our setup, in which changes in the level of investor protection have an impact on capital accumulation via changes in the number of entrepreneurs.

In Castro, Clementi, and MacDonald [2003] we consider one such variation. We allow production to depend on labor as well as capital, and young individuals to choose whether to become entrepreneurs or to work for a wage; the fraction of entrepreneurs is an equilibrium outcome. Poorer investor protection can now be accommodated to some degree by an increase in the fraction of entrepreneurs. This increase will lower the capital available to each entrepreneur. In turn, this will mitigate the increase in risk borne by the entrepreneurs themselves, and so lower their expected income. We show that the economy does adjust along this new margin. However, in general, the negative association between investor protection and capital accumulation still holds.

A different model allows for credit rationing. Consider our baseline model, but assume that running a project requires incurring a fixed cost and that individuals are heterogeneous with respect to its magnitude. If an agent’s cost is too high for his project to be financed, he will resort to a subsistence activity that yields a constant outcome. In this environment an improvement in investor protection may increase the size of the entrepreneurial sector. The net effect on capital accumulation, however, is still uncertain, because the supply effect will still be at work: with a larger entrepreneurial sector each entrepreneur will bear less risk and will receive a lower return. In turn, this implies that he will save less.

In the Introduction, we mentioned that our paper is not the first to investigate the effect of moral hazard on capital accumulation. Among the studies that have addressed the same question, the one by Khan and Ravikumar [2001] is most similar to ours. Thus, it is striking that their results are very different. Also in
their setup, the introduction of moral hazard leads to imperfect risk sharing. Its effect on capital accumulation, however, has the opposite sign. In our framework the positive impact on savings that is associated with poorer risk sharing is induced by a redistribution of resources toward agents having a higher propensity to save. By assuming that agents are infinitely lived, Khan and Ravikumar rule out this mechanism. In their setup, there is no distinction between entrepreneurs and owners of capital. It appears that some heterogeneity in the propensity to save is a necessary condition for a model with infinitely lived agents to generate results qualitatively similar to ours. Finally, note that while we focus on short-term contracts, Khan and Ravikumar allow for long-term contracts. Short-term contracts ignore the adverse effect that higher savings today (higher capital tomorrow) have on the provision of incentives for future generations. As discussed in Appendix 1, long-term contracts do take this effect into account. In the same appendix we show that even in an OLG model, if there exist infinitely lived institutions that provide individuals with lifetime optimal risk sharing and financing contracts, then moral hazard invariably leads to lower capital accumulation. We also argue that such contracts will be feasible only under very restrictive assumptions.

IV. THE ROLE OF INTERNATIONAL CAPITAL MOBILITY

We now consider a small open economy with no restrictions on capital flows. The old may now lend to foreigners, and the intermediaries may borrow from abroad. The interest rate is the rate prevailing internationally, and any difference between domestic demand and supply of capital is closed by an instantaneous flow of capital. In fact, the economy is always in steady state.

Since the worldwide supply of capital is infinitely elastic, there is no supply effect. Thus, poorer investor protection invariably translates into domestic entrepreneurs demanding less capital. In turn, this implies a lower domestic supply of capital and lower steady state levels for capital and output.

Let $k^d$ be the capital demanded by domestic intermediaries, and employed in production, and let $k^s$ be the total capital supplied by the currently old generation. The difference $k^s - k^d$ corresponds to the net outflow of capital from the domestic economy, i.e., to the deficit on the capital account. Proposition 3
establishes that, provided the level of investor protection is beyond a certain threshold, poorer investor protection is associated with a larger deficit (lower surplus) of the capital account.

**Proposition 3.** There exist unique capital levels $k^*$ and $k^{**}$, with $0 < k^{**} < k^*$, such that

1. If $k^d \leq k^*$, then $k^s - k^d \geq 0$;
2. If $k^d \leq k^{**}$, then $\partial(k^s - k^d)/\partial\xi \leq 0$.

**Proof of Proposition 3.** 1. Given a level of capital in domestic production $k^d$, we know from Section III that the level of capital supplied by the old generation is determined by the market-clearing condition $k^s = k^s(k^d) \equiv \kappa(r)[\bar{z}f(k^d) - (r + \delta)k^d]$. Since $\kappa(r)$ is a constant, $k^s(k^d)$ has the same shape as the intermediary’s budget constraint, which was introduced previously. Figure VII plots this function together with the 45 degree line.

Notice that the vertical difference between $k^s(k^d)$ and the 45 degree line corresponds to the net capital outflow from the domestic economy. Define $k^*$ such that $k^* = k^s(k^*)$. It follows that $k^* > 0$ exists and is unique. The first part of the proposition then follows.

2. Note that, by Proposition 1, $k^d = D(r,\xi)$ is strictly
creasing in $\xi$. Therefore, $k^d \leq D(r,0)$. Now define $k^{**}$ such that
$\frac{\partial k^*(k^{**})}{\partial k^d} = 1$. It follows that $k^{**} > 0$ exists and is unique. Clearly, $k^{**}$ maximizes $k^* - k^d$, and $k^{**} < k^*$. For $k^d \leq k^{**}$ we have
$\frac{\partial(k^* - k^d)}{\partial k^d} \geq 0$. Since $k^d$ is strictly decreasing in $\xi$, the
second part of the proposition follows. QED

In Section III we showed that poor investor protection can
have a positive effect on savings via the adjustment of the interest
rate. For a closed economy, this effect can be stronger than the
negative effect on capital demand. In this section we considered a
small open economy with unrestricted capital flows. The general
equilibrium effect vanishes, leaving only the demand effect.
Therefore, better investor protection is always associated with
higher savings. Better investor protection also implies higher
welfare for all generations.

V. Data

In this section we provide empirical evidence about the key
implications of our model. We measure investor protection with
the indicators introduced by La Porta, Lopez-de-Silanes, Shleifer,
and Vishny [1998]. Such indicators quantify explicit protections
awarded to shareholders and creditors by corporate, bankruptcy,
and reorganization laws, as well as the quality of law enforce-
ment. We focus on four of them. The variable $CR$ is an index
aggregating different creditor rights in firm reorganization and
liquidation upon default. The indicator antidirector rights, AR,
and the dummy one share-one vote, OV, are two indices of share-
holder rights geared toward measuring the ability of small share-
holders to participate in decision-making. Finally, the index rule
of law, RL, proxies for the quality of law enforcement. The vari-
ables are described in detail in La Porta, Lopez-de-Silanes, Shlei-
fer, and Vishny [1998].

V.A. Risk-Sharing

The analysis in subsection III.B implies that when investor
protection is imperfect, companies’ insiders face an incentive to
expropriate resources from outside investors. This incentive is
stronger the lower is the level of investor protection. Investors’

14. Without loss of generality, Figure VII depicts the case in which $k^* < D(r,0)$. Depending on $r$, in particular, it is possible to have $k^* \geq D(r,0)$ as well.
optimal response to the adverse incentives induced by imperfect protection is to require repayment terms that are less tied to the state realizations. In other words, our model predicts that in countries characterized by better investor protection, insiders should be able to transfer a larger share of their idiosyncratic business risk to better-diversified outside investors. Our purpose here is to explore the empirical association between investor protection and risk sharing. In the absence of a direct measure of risk sharing, we study how capital structure and ownership concentration, respectively, vary with the levels of investor protection in the cross section of countries. The reason is that, all else being equal, the risk borne by company insiders should be larger, the larger the company’s leverage and the higher their ownership stakes. In fact, based on the features of standard debt and equity contracts, shareholders’ risk is increasing in leverage. The portion of this risk that shareholders actually bear depends on how diversified their portfolios are. All else equal, the level of diversification will be lower the higher their ownership stake. To summarize, we conjecture that insiders’ risk sharing is poorer in countries where debt accounts for a larger fraction of external finance and where ownership concentration is higher.

For a subset of the countries included in the investor protection data set, the Financial Structure database assembled by Beck, Demirgüç-Kunt, and Levine includes data on the value of outstanding debt and equity in the years 1990 through 1996. We use these data to compute the average fraction of external finance that is accounted for by debt. This fraction is negatively correlated with the indicators of investor protection. The correlation coefficients are $-0.65$ for $AR$, and $-0.39$ for $CR$. The corre-
sponding $p$-values are 0.0358 and 0.0002, respectively. We interpret these findings as empirical support for our prediction.\footnote{Our decision to combine bonds and bank loans in one measure of debt may bias our results. The reason is that the risk-sharing properties of the two instruments might be different. We refer to the view that sees banks as effective risk-sharing providers. As an alternative measure of leverage, we considered the ratio between the value of outstanding bonds and total market finance (i.e., the sum of bonds and equity finance). We found a robust negative correlation between this measure and the different indicators of investor protection.}

We now turn to ownership concentration. Our model implies that ownership should be more concentrated in countries with poorer protection. This is exactly what is found by La Porta, Lopez-de-Silanes, Shleifer, and Vishny [1998]. They report a negative correlation between their indicators of investor protection and a measure of ownership concentration given by the mean (or median) combined equity stake for the three largest shareholders of the ten largest nonfinancial, domestic, totally privately owned, and publicly traded companies.

\textit{V.B. Investor Protection, International Capital Mobility, and Growth}

The second key implication of our model is that the effect of investor protection on growth should depend on international capital mobility. The analysis carried out in Section III implies that if we were to observe two countries, completely closed to capital flows, that differed only in terms of investor protection, then we should observe the economy with poorer protection to grow faster. That is, for perfectly closed economies, investor protection should have a conditional negative effect on growth. In Section IV we showed that, in the polar case in which a country is completely open to capital flows, different levels of investor protection have no effect on rates of return. For perfectly open economies our model implies that countries with better protection should have higher steady states.

Most national economies are better described by models allowing for some, albeit incomplete, restrictions on capital flows rather than by either of the extremes considered above. As long as some restrictions are in place, the domestic interest rate is not completely determined by the rate prevailing abroad, and the model displays a transition to the steady state. Lower levels of investor protection are still reflected in lower paths of the interest rate. Most importantly, the adjustment of the interest rate and the strength of the general equilibrium effect on supply will be...
larger, the tighter are the constraints on capital flows. Thus, our
theory predicts that the positive effect of investor protection on
growth should be larger for countries that impose milder restric-
tions on capital flows.

Our goal is to determine whether the data are consistent
with the empirical prediction just outlined. We first conduct a
statistical analysis of cross-sectional data on growth, investor
protection, and openness, and then explore the development ex-
periences of South Korea and India.

To build a measure of restrictions on capital movements, we
follow Alesina, Grilli, and Milesi-Ferretti [1994]. For each coun-
try, we construct a time-series dummy based on the IMF’s Annual
The dummy variable takes the value of 1 for a given country in a
given year if the IMF finds evidence of restrictions on payments on
capital transactions for that country-year pair. Such restrictions
include both taxes and quantity restrictions on the trade of for-

eign assets. We compute the average of this dummy over the
sample period to obtain a measure of the fraction of time each
country imposed restrictions on international capital transac-
tions; this is our variable $RCT$. There are few countries for which
the dummy varies significantly over time. $RCT$ is equal to one for
just over one-third of the countries in our data, and is roughly
uniformly distributed for the rest. Since $RCT$ does not capture
either the kind or the severity of capital market restrictions
imposed, or even whether the type of restrictions imposed re-
mained constant over time, it is a very rough measure of restric-
tions on capital transactions.\(^{17}\)

Figure VIII illustrates how the relation between investor
protection and growth varies across closed and open economies.
In the two panels we plot two measures of investor protection
against the growth rate of GDP per worker for two sets of coun-
tries: those with values of $RCT$ that belong to the bottom quartile
of the cross-sectional distribution of this variable (“open” coun-
tries) and those with values of $RCT$ that belong to the top quartile
of the cross-sectional distribution of this variable (“closed” coun-
tries).\(^{17}\)

\(^{17}\) Recently, Dennis Quinn has constructed alternative measures of inter-
national financial regulations by coding the provisions of domestic and interna-
tional laws of 64 countries from 1950 to 1997. (See Quinn [1997] for a detailed
illustration of his methodology.) Quinn’s measure of capital market restrictions,
CAPITAL, accounts for the severity of the restrictions at the cost of a greater
discretion in construction of the indicator. When repeating our analysis substi-
tuting CAPITAL for $RCT$, we obtain very similar results. Since the correlation
between $RCT$ and CAPITAL is 0.77, this is not surprising.
tries), and those whose values fall in the top quartile ("closed").

Our model predicts that the correlation between investor protection and growth should be higher among open economies. The plots are consistent with this prediction. For closed economies, the slopes are not significantly different from zero.

Figure VIII also identifies the countries that are mostly responsible for the sample correlations. Among open economies, the fast growers have the right institutions: Hong Kong, Malaysia, Indonesia, and Singapore. Among the closed ones, instead, there are several with good institutions that do not grow nearly so fast. What is striking is that the fast growers among the closed economies are those with poor investor protection: Korea, Taiwan, and Thailand. Obviously, we are not the first to partition East-Asian

18. The IMF does not provide data on capital restrictions for Taiwan. Nevertheless, based upon the capital account liberalization chronology for this country, described in detail in Kaminsky and Schmukler [2003], we classify it as closed and include it in the plots. As it is the case for Korea, Taiwan completed the liberalization of international capital flows only at the end of the 1990s. The significance of our results is not sensitive to the inclusion of Taiwan; indeed, we do not include it in our regression analysis.

19. In Figure VIII we restrict our attention to the relationships between growth and the variables $AR$ and $CR$, respectively. We think that these are the two indicators that are most likely to reflect the level of overall investor protection. However, we recognize that the role of $RL$, which proxies for the level of law enforcement, may also be important. Therefore, we computed a summary measure of protection using principal components. In our case, the principal components are four orthogonal vectors that are computed as linear combinations of the four series $AR$, $CR$, $RL$, and $OV$. The summary measure is the weighted average of the components, where each weight is the proportion of the variation in the original series that is explained by the related component. Plotting the growth rates against the new measure yields results that are similar to those illustrated in Figure VIII. That is, for open economies the correlation coefficient is significantly higher. In the regression analysis that follows, we consider all four protection indicators.
economies into fast- and slow-growers. What we find remarkable is the way in which the differences in growth rates are associated with differences in investor protection and openness, a way that is quite consistent with our theory.

In order to condition on other potential sources of cross-country variation in growth rates, we now consider a standard growth regression framework. Our regressors are the indicators of investor protection and of restrictions on capital transactions, as well as their interactions:

\[ GR_i = \alpha + \phi' IP_i + \gamma RCT_i + \varphi' (IP_i \times RCT_i) + \theta' X_i + \varepsilon_i, \]

where \( GR_i \) is the average annual growth rate of income for country \( i \), \( IP_i \) is a set of indicators of investor protection, \( RCT_i \) is a measure of restrictions on capital transactions, \( X_i \) is a vector of other conditioning variables believed to be important to account for growth, and \( \varepsilon_i \) is the error term.

When the restrictions \( \gamma = 0 \) and \( \varphi = 0 \) are imposed, the model relates investor protection to income growth without any reference to the mechanism through which the former influences the latter. In other words, the restricted regression summarizes the combined evidence of La Porta, Lopez-de-Silanes, Shleifer, and Vishny [1997], King and Levine [1993a, 1993b], and others in a reduced-form way. Their finding that investor protection fosters financial market development, which in turn is positively associated with growth, corresponds to a significantly positive estimate of \( \phi \).

Our theory suggests that the overall positive effect of investor protection on growth may be decomposed into a positive effect (our partial equilibrium demand effect), captured by \( \phi \) in the unrestricted regression, and a negative effect that depends on the restrictions on international capital movements (our general equilibrium effect on supply), captured by \( \varphi \).

In deciding which variables to include in \( X_i \), we choose to remain anchored to our theory as much as possible. Therefore, we only include the natural logarithm of initial income as a condi-

20. Notice that our specification is more general than one that uses the income level as dependent variable. As noticed by Mankiw, Romer, and Weil [1992], if the dependent variable was the level of income instead of its growth rate, we would implicitly assume that countries deviate only randomly from their steady states. Our approach can also account for out-of-steady-state dynamics.
Our income data are real GDP per worker from the Penn World Tables, version 6.1. Our set of countries corresponds to the 49 in La Porta, Lopez-de-Silanes, Shleifer, and Vishny [1998] except for Germany, which has missing income data for most years, and for Jordan and Venezuela, which have missing data on creditor rights. In the unrestricted regression we also drop Switzerland, Zimbabwe, and Taiwan, because the IMF did not include them in its survey in every year. The time span of our sample is from 1967 to 1996, the largest possible for all 49 countries in the La Porta, Lopez-de-Silanes, Shleifer, and Vishny [1998] data set.

We report our results in Table I. The first column refers to the restricted regression. Consistent with the existing literature, we find that two of the measures of investor protection have significantly positive coefficients. The estimated impact of investor protection is large. One standard deviation increase in $RL$ is associated with a 1.12 percent increase in the growth rate of income, i.e., almost 50 percent of the average annual growth rate in the sample, 2.3 percent. Since we find a significant effect when conditioning on initial incomes, we conclude that countries with better investor protection also tend to have higher income levels (not only growth rates).

The second column presents estimates of the unrestricted model. All four coefficients of the investor protection variables are positive (although with varying degrees of statistical significance), and three of the coefficients of the interaction terms are negative. The fourth coefficient is positive, but the $p$-value for the hypothesis that it is equal to zero is 0.51. These results are consistent with our theory in the following sense. If a country has never imposed restrictions on capital transactions over the relevant time period, so that $RCT = 0$, then investor protection is clearly positively associated with growth. To the extent that $RCT = 0$ corresponds to the highest degree of openness in the data, our model suggests that we interpret the positive estimates of $\phi$ as capturing the partial-equilibrium effect on demand. As $RCT$ increases toward 1, however, the regression results show

21. The results in Table I did not change in any important way when we included in $X_i$ schooling measures based upon the Barro and Lee [1996] data set (we tried both the log of average secondary schooling and the log of average total schooling). With log schooling and log initial income, our $X_i$ becomes the "simple information conditioning set" considered by Beck, Levine, and Loayza [2000a, 2000b].
that the overall effect of investor protection on growth diminishes. This is consistent with an increased importance of the general-equilibrium effect on supply.

Creditor rights seem to have the largest impact on growth. The coefficients of $CR$ and $CR \times RCT$ are statistically significant, and the $p$-value for the null hypothesis that they are jointly insignificant is 0.028. In the absence of capital market restrictions (i.e., $RCT = 0$), a one standard deviation increase in $CR$ is predicted to increase the growth rate by 1.38 percent. At the other extreme (i.e., $RCT = 1$), the predicted effect of the same change

<table>
<thead>
<tr>
<th>Dependent variable: average annual growth rate of real GDP per worker 1967–1996</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Log Real GDP per worker 1967</td>
<td>$-0.01392^{**}$</td>
</tr>
<tr>
<td></td>
<td>(0.00568)</td>
</tr>
<tr>
<td>One share-one vote (OV)</td>
<td>$0.00854^{***}$</td>
</tr>
<tr>
<td></td>
<td>(0.0046)</td>
</tr>
<tr>
<td>Antidirector rights (AR)</td>
<td>$-0.0048$</td>
</tr>
<tr>
<td></td>
<td>(0.00125)</td>
</tr>
<tr>
<td>Creditor rights (CR)</td>
<td>$0.00149$</td>
</tr>
<tr>
<td></td>
<td>(0.00174)</td>
</tr>
<tr>
<td>Rule of law (RL)</td>
<td>$0.004195^*$</td>
</tr>
<tr>
<td></td>
<td>(0.00134)</td>
</tr>
<tr>
<td>Restrictions on capital transactions (RCT)</td>
<td>0.04768$^{***}$</td>
</tr>
<tr>
<td></td>
<td>(0.02538)</td>
</tr>
<tr>
<td>OV $\times$ RCT</td>
<td>0.0091</td>
</tr>
<tr>
<td></td>
<td>(0.01362)</td>
</tr>
<tr>
<td>AR $\times$ RCT</td>
<td>$-0.0053^{***}$</td>
</tr>
<tr>
<td></td>
<td>(0.00298)</td>
</tr>
<tr>
<td>CR $\times$ RCT</td>
<td>$-0.0103^{**}$</td>
</tr>
<tr>
<td></td>
<td>(0.00422)</td>
</tr>
<tr>
<td>RL $\times$ RCT</td>
<td>$-0.00101$</td>
</tr>
<tr>
<td></td>
<td>(0.00237)</td>
</tr>
<tr>
<td>Constant</td>
<td>$0.1209^*$</td>
</tr>
<tr>
<td></td>
<td>(0.04892)</td>
</tr>
</tbody>
</table>

Number of countries | 46 | 43 |
Adjusted $R^2$ | 0.326 | 0.345 |

White robust standard errors are in parentheses. 

* Significant at 1 percent; ** Significant at 5 percent; *** Significant at 10 percent.

is actually a small decline in growth, $-0.04\percent$; the supply effect is stronger than the more familiar demand effect. The strength of the interaction with $RCT$ explains why, in the restricted regression, $CR$ appears unimportant for growth.\textsuperscript{22}

The findings are similar, but less statistically and economically significant, for the impact of $RL$. The coefficients of $RL$ and of its interaction with $RCT$ are not individually statistically significant, but the hypothesis that both are zero has a $p$-value of 0.09. A one standard deviation increase in $RL$ is predicted to increase growth by 0.97 percent when $RCT = 0$ and by 0.71 percent when $RCT = 1$. This is consistent with a significant positive coefficient in the restricted model.\textsuperscript{23}

The reader may wonder whether the regression results are driven by outliers. In Figure IX we plot the partial relationships between income growth and the interaction terms $AR \times RCT$ and $CR \times RCT$, respectively. It appears that outliers do not play any significant role. The signs of the relationships seem to hold for the broad sample of countries.

One would also like to know whether our results are robust to the choices of regression specification and data set. In this respect, it is helpful to recall the results of other recent studies, namely Arteta, Eichengreen, and Wyplosz [2001] and Chinn and

\textsuperscript{22} The fact that $OV$ is marginally significant in the first regression also appears to be an artifact of the restrictions imposed. In the unrestricted model, the coefficients of both $OV$ and $OV \times RCT$ are insignificant, and the $p$-value for the hypothesis that both are zero is 0.24.

\textsuperscript{23} The results also suggest the effect of $AR$ on growth operates through the supply effect, but the evidence is weak. The coefficients on $AR$ and $AR \times RCT$ are small and statistically insignificant: the hypothesis that they are both zero has a $p$-value of 0.22.
Ito [2002], that employ alternative specifications (in particular, different conditioning variables) and data sets. Differently from ours, the ultimate goal of these studies is to investigate the statistical relationship between capital account liberalization and various measures of development, and to understand whether such a relationship depends on the quality of institutions. In spite of this difference, their results can be reinterpreted as showing that the magnitude of the (positive) impact of investor protection on development depends negatively on the extent of capital restrictions.

We now take a closer look at the development experiences of two countries: South Korea and India. Korea is one of the post-World War II growth miracles. During our sample period, its GDP per worker grew at an astonishing 6.06 percent annual compounded rate, among the highest in the world. Despite a lower initial level of PPP-adjusted GDP per worker, India grew only at a 2.95 percent rate, a slightly above average performance in our sample. What accounts for such difference? Country growth performances in Far East Asia in the second postwar period have varied widely. A large literature has tried to explain this heterogeneity. Most studies argue that the variation was caused either by differences in government policies, or by other idiosyncratic factors. We focus on Korea and India because there is ample evidence suggesting that, at least from a qualitative point of view, the growth-promoting policies enacted in these two countries were very similar. We suggest that the relevant difference between the two is in terms of institutions and, in particular, in terms of investor protection.

India and Korea appear to differ greatly in terms of investor protection. According to legal scholars, India, a British colony until 1947, belongs to the common-law family. Korea’s laws and institutions, instead, are inspired by the civil law tradition, and are modeled on the German example. As a result, Korea ranks significantly lower than India in terms of both the AR and CR indicators. These observations lead us to conclude that India is

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24. The dependent variable in Chinn and Ito [2002] is the change in indicators of financial market development rather than the growth rate of income.

25. However, India scores slightly lower in terms of law enforcement. Our impression, based upon anecdotal evidence, is that investors are overall better protected in India. When we performed the principal component analysis described in footnote 19, India did come out as having a better summary index of investor protection than Korea (and also better than Thailand and Taiwan).
more likely than Korea to provide outside investors with effective protection from the exploitation of insiders.

Both the Korean and the Indian governments have played very active roles in the allocation of credit to firms. A common theme of their interventions in the financial sector has been the creation of rents for specific manufacturing sectors. Such rents were created by inducing banks and other financial intermediaries to keep the returns to investors artificially low in order to provide selected industries with credit at very favorable terms. This policy was feasible thanks to very tight controls on capital flows. Such controls were gradually eased during the last years of our sample period. However, there is no doubt that domestic investors were barred from investing abroad during most of the period. Domestic capital was kept captive. Referring to Korea, Dornbush and Park [1987] argue that “... By paying depositors low real interest rates and by controlling capital outflows, the government implicitly taxed depositors, then channelled the proceeds to favored sectors for investment.” Then, why did such a policy, often referred to as one of financial repression, succeed in promoting growth in Korea but fail in India?

The literature provides several tentative answers to this question. Cho and Vittas [1995], for example, argue that the Korean government made better choices in terms of which sectors to privilege. Others have argued that, differently from their Indian counterparts, Korean firms have been subject to foreign competition, with the result of achieving higher productive efficiency. Our stand is that these explanations fail to account for another crucial difference between the two development experiences: the one between saving rates.

A high national saving rate is a well-known feature of the

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26. There is ample consensus on the view that the credit policies enacted in India and Korea were very similar, at least in spirit. For example, according to Cho and Vittas [1995], this is the general view that emerged from the World Bank research project titled “Effectiveness of Credit Policies in East Asian Countries.”

27. Both Korea and India are in the bottom quartile of the cross-country distribution of our measures of openness to international capital flows. The IMF finds that both countries had restrictions in place in all years of our sample. Therefore, our variable RCT takes value 1 (the maximum value) for both. The measure proposed by Quinn yields a consistent characterization. The average of his indicator CAPITAL, which ranges from 0 (completely closed) to 4 (perfectly open), is 1.4 for India and 1.7 for Korea.

28. A further confirmation that this was the case for Korea is provided by Dornbush and Park [1987]. They report data from the IMF’s International Financial Statistics showing that in the 1980s nonbank Korean residents had almost no external deposit holdings.
Korean growth experience, and it helps explain how Korea was able to sustain a very high investment rate since the late 1960s. Precisely, Young [1995] identifies capital accumulation as the key ingredient behind the tremendous growth of Korea’s GDP. The average Korea’s saving rate in our sample was 28 percent, while India’s was just 19 percent. Moreover, Korea’s rate was substantially higher in any single year. The size of the gap between saving rates looks even more dramatic when we consider that, according to several measures, average real interest rates have been higher in India than in Korea. The IMF’s International Financial Statistics (IFS) provide yearly measures of several key nominal interest rates for developing countries. Unfortunately, rates on time deposits are available only for Korea. Dornbush and Park’s [1987] comment on these data is that “...Although Korea is often cited as an example of successful financial liberalization with high and positive real interest rates mobilizing financial resources for investment and growth, ... real rates have not been high, except in 1965–69, ... The relationship between saving and interest rates remains unresolved in Korea, just as everywhere else.” The IFS data set, however, does contain information on prime nominal annual lending rates of commercial banks for both countries. Real rates (i.e., nominal rates adjusted for realized inflation) were, on average, 7 percent in India and only 3.2 percent in Korea. One problem with these data is that they are limited to 17 observations (from 1980 to 1996). An alternative is to follow Hsieh [2002] and look at discount rates, for which we have data for the whole sample period in the IFS. We find discount rates in India to be on average significantly higher than in Korea: 2.2 percent versus –0.56 percent. How to reconcile the behavior of saving rates with observed interest rates? Our theoretical analysis suggests that lending rates were lower (rates of return to entrepreneurs were higher) in Korea because risk sharing was poorer.

In both countries, the purpose of the government was to entice entrepreneurs to invest, by allowing them to borrow at low rates. Our point is that in setting those rates, either government

29. We computed the saving rate as the ratio of nominal saving to nominal GDP, where nominal savings are given by nominal GDP minus the sum of nominal private consumption and nominal government consumption. Nominal values are in domestic currency. The data are drawn from the national account information contained in version 6.1 of the Penn World Tables.

30. For Korea, in particular, Hsieh [2002] finds discount rates to be approximately equal to deposit rates.
must have taken demand conditions into account. The higher the undiversifiable risk entrepreneurs were subject to, the lower the rates needed to be in order to accomplish the government’s objective. Since, as we argue below, the institutional framework provided Indian entrepreneurs with better opportunities for risk sharing, the latter required a lower return on investment than their Korean analogues. This implies that the Indian government could allow interest rates on loans to be higher than in Korea, thereby limiting the extent of the income redistribution in favor of the entrepreneurial sector. Finally, this contributed to keeping the saving rate in India relatively low.

We have already argued that measuring risk sharing is not an easy task. However, the proxies introduced in subsection V.A suggest that Korean entrepreneurs had a harder time sharing business risk with the rest of the population. Consider capital structure choices first. Korean firms’ leverage has been much higher than their Indian counterparts’ throughout our sample period. It has been repeatedly argued in the literature that the Korean government kept ready to avoid that and this resulted in (possibly inefficient) bankruptcies. However, even if firms were provided insurance against extreme events, a larger fraction of fixed income claims must have implied greater income risk for shareholders. The fraction of this risk that was actually borne by them depended on their ability to diversify their portfolios. In order to assess the diversification opportunities available to insiders, we consider data on ownership concentration. In general, the presence of pyramidal schemes and intragroup cross-shareholdings makes it inaccurate to measure cash-flow rights by simply considering direct shareholdings.

31. This fact has been documented by several authors, using different data. Claessens, Djankov, and Xu (2000) compute leverage ratios using data drawn from the annual reports of the companies listed on the major stock exchanges, as gathered by the Worldscope Database. They find that during the period 1988–1996 Korean companies were the most leveraged in their large sample of developed and developing countries. This ranking is preserved even when the last two years of the sample, characterized by an accelerated debt buildup in Korea, are excluded. Indian companies instead lie in the left tail of the cross-country distribution of leverage. A similar picture emerges when we consider the data on the ratio of debt to external finance introduced in subsection V.A. The fraction of total external finance accounted for by debt is 83 percent in Korea and 67 percent in India.

32. A pyramidal structure allows an individual to have cash-flow rights on a company via ownership of a third company. The simplest case is the one in which a person has an ownership stake in a firm, which in turn holds a stake in a third company. The simplest example of cross-shareholdings is given by the case in which two companies hold ownership stakes in each other.
compute the total cash-flow rights of ultimate owners, direct cash-flow rights constitute only a lower bound. That is, the presence of both pyramids and cross holdings lead to the underestimation of ownership stakes. We argue that in Korea’s case, the bias introduced by using direct rights is particularly large. The reason is that cross shareholdings are a pervasive feature of chaebols, Korean business groups. Nam, Kim, Kang, Joh, and Kim [2001] find that in 1997 the average direct ownership fraction of the largest shareholder of the 10 biggest chaebols was a mere 10.29 percent. When properly accounting for cross shareholding, Nam, Kim, Kang, Joh, and Kim find that this figure climbs to a staggering 39.58 percent. The available evidence suggests a very different scenario for Indian firms. Goswami [2002] writes that in India “. . . During the industrial expansion of the 1970s and 1980s, the average share ownership of the controlling groups declined to 15 percent.” Bertrand, Mehta, and Mullainathan [2002] report that in their sample the average equity stake of directors was 16.7 percent (7.45 percent for business groups and 22.99 percent for stand-alone firms). Unfortunately for our analysis, these figures refer to direct holdings only. This makes it hard to compare them with the numbers reported by Nam, Kim, Kang, Joh, and Kim about Korean firms. However, if, as it seems plausible, in the Bertrand, Mehta, and Mullainathan data set the directors include the largest shareholders, their indirect cash-flow rights must be lower than the direct ones. Therefore, 14.9 percent (2 × 7.45 percent) constitutes an upper bound for the total cash-flow rights of directors in Indian business groups. Our conclusion is that, at least for large groups, the concentration of cash-flow rights was much higher in Korea than in India.

The difference in risk sharing that we have documented is clearly consistent with our theory. Given the evidence on investor protection, our model predicts that Indian entrepreneurs should have been able to share their business risk with the population to a larger extent than their Korean counterparts.

To summarize, the comparison of India’s and South Korea’s

33. The result is consistent with what is reported by La Porta, Lopez-de-Silanes, Shleifer, and Vishny [1998]. They find that the average direct ownership fraction of the three largest shareholders of the 10 biggest chaebols is 23 percent.
34. Bertrand, Mehta, and Mullainathan [2002] draw their data from Prowess, a database that includes annual report information for Indian companies between 1989 and 1999. Their sample contains about 18,500 firm-year observations.
development experiences nicely illustrates the key mechanism at work in our model. The evidence tells us that during the sample period both countries have placed considerable restrictions on capital flows, and that India has better protected the interests of investors than Korea. In turn, this difference in investor protection seems to be reflected in a substantial difference in the opportunities for risk diversification available to entrepreneurs in the two countries. The data also tell us that during the same period Korea grew much faster and had much higher saving rates than India, despite lower real interest rates. Our theory provides a rationalization for this set of findings. The purpose of both the Korean and the Indian government was to direct funds to the entrepreneurial sector at favorable terms, with the purpose of fostering investment in given industries. Real interest rates (returns to entrepreneurs) in Korea were lower (higher), because entrepreneurs faced more risk and therefore needed greater incentives in order to invest. In turn, this has implied the distribution of larger rents to the entrepreneurial sector. Finally, given the higher saving rate of entrepreneurs, this led to higher saving and faster capital accumulation.

VI. Conclusion

In this paper we introduced investor protection in the familiar two-period OLG model of capital accumulation. Our objective was to assess the widely believed notion that investor protection fosters economic growth, in a model suitable for answering questions about aggregates, i.e., a general equilibrium model.

Our model produces several interesting implications. First, the structure of financial claims adjusts endogenously to changes in investor protection. We show that the risk sharing implied by optimal financing contracts is increasing in the level of protection. We find empirical support for this prediction. In countries where outside investors are better protected, equity claims are more prevalent, and firm ownership is less concentrated.

Second, we show that the overall effect of protection on capital accumulation can be decomposed into a positive effect on the demand for capital, and a negative general equilibrium effect on supply. The strength of the supply effect is greater the tighter are the restrictions on international capital mobility. Therefore, our model predicts that the positive effect of investor protection on growth should be larger for countries that impose lower restric-
tions on capital flows. We also find the data to be consistent with this prediction.

Our analysis can be extended in several potentially interesting ways. One is to introduce imperfect contract enforceability. This is of interest because some empirical measures of investor protection that appear to be associated with growth reflect the ability of the legal system to ensure that contracts are honored. It would also be interesting to introduce inside equity in the model, with the purpose of studying how the relative importance of inside and outside sources of finance vary with the degree of investor protection. Finally, endogenizing the level of investor protection would open the possibility of understanding which features of actual economies can account for the large cross-country variation in this variable.

We can also ask whether our analysis provides any insight into the recent wave of accounting-related scandals in the United States. Interpreting these events, journalists and commentators appear to describe the breakdown of a separating equilibrium in a simple adverse selection model. They argue that firms involved in the scandals were inefficient firms whose managers found it optimal to mimic the behavior of better-performing companies. Our model suggests a very different interpretation. Suppose that the strong economy of the 1990s led to an increase in what the model describes with $z_h$, but that incentives in contracts did not adjust immediately, or did not adjust enough. The model suggests that the firms involved in the scandals are actually the ones that had been performing well, and in which insiders found it profitable to appropriate some of the cash flows, disguising this appropriation by misreporting their accounting numbers. These firms are now (i.e., $t + 1$) less valuable than they were earlier thought to be, not necessarily because they are less productive than expected (although this, too, would be consistent with the model, i.e., $z_{t+1} = z_f$). Instead, the reason is that contractual incentives lagging business conditions made taking a chance at appropriating large parts of firm resources optimal for firm managers. The effect of managers’ expropriation on firm value was aggravated by the fact that such activity was inefficient, in that resources were used up in the hiding process, so that value concealed from investors did not translate one to one into higher managerial wealth. Accounts of the recent history of companies such as Tyco and Global Crossing lend plausibility to this idea.
APPENDIX 1: LONG-TERM CONTRACTS

In this appendix we characterize the allocation that would be chosen by a social planner that attaches a weight \( \gamma \), \( \gamma \in (0,1) \), to the utility of the generation born in period \( t \). We show that this allocation satisfies Rogerson’s [1985] condition on the intertemporal allocation of consumption. By construction, any market mechanism that relies on one-period financing contracts violates this condition. Therefore, the allocation that we have studied in Section III falls inside the Constrained-Pareto frontier. However, following an argument introduced by Allen [1985], we show that two-period contracts actually collapse to one-period arrangements if we introduce the possibility of unmonitored borrowing and lending.

The timing of the interaction between the planner and an individual born at time \( t \) is as follows. At the beginning of time \( t \), the planner makes a capital advance \( k_t \); its investment yields \( z_t f(k_t) \). Then, the agent reports \( z_h \) or \( z_l \), and surrenders \( z_h f(k_t) \) or \( z_l f(k_t) \) to the planner. Finally, the planner assigns a lifetime consumption allocation \( (c^x_{i,t}(\hat{z}_t), c^{o}_{i,t+1}(\hat{z}_t))_{t=0}^{\infty} \). For every \( t \), the pair \( (c^x_{h,t}, c^{o}_{h,t}) \) denotes the consumption allocation intended for agents born at time \( t \), conditional on high and low reports, respectively. The pair \( (c^x_{l,t}, c^{o}_{l,t}) \) denotes the time \( t \) consumption allocation intended for agents born at time \( t-1 \), again conditional on their report (issued at time \( t-1 \)).

Given initial capital, \( k_0 > 0 \), the planner’s optimization problem is

\[
\max_{c^x_{0},(c^x_{l,t},c^{o}_{l,t+1});t=0} \gamma^{-1} u(c^o_0) + \sum_{t=0}^{\infty} \gamma^t \left\{ \rho \left[ u(c^x_{h,t}) + \beta u(c^{o}_{h,t+1}) \right] + (1 - \rho) \left[ u(c^x_{l,t}) + \beta u(c^{o}_{l,t+1}) \right] \right\},
\]

subject to

(12) \( \rho (c^x_{h,t} + c^{o}_{h,t}) + (1 - \rho) (c^x_{l,t} + c^{o}_{l,t}) = \tilde{z}_t f(k_t) \)

\[\quad + (1 - \delta) k_t - k_{t+1} \quad \forall \ t \geq 0,\]

(13) \( u(c^x_{h,t}) + \beta u(c^{o}_{h,t+1}) \geq u(c^x_{l,t}) + \xi \Delta f(k_t) + \beta u(c^{o}_{l,t+1}) \quad \forall \ t \geq 0.\]

Equation (12) is the resource constraint, and condition (13) is the incentive-compatibility constraint, conditional on high output. It is easy to show that (13) will always bind at the optimum.
Start with the $\xi = 0$ case. In this case, the planner’s solution is to provide full insurance. In fact, the following holds at all times:

\begin{equation}
    u'(c^*_t) = \beta[\bar{z}f''(k_{t+1}) + (1 - \delta)]u'(c'^*_t)
\end{equation}

and

\begin{equation}
    u'(c^*_t) = (\beta/\gamma)u'(c'^*_t).
\end{equation}

The steady-state capital stock is then determined by the modified golden rule condition,

\[ \bar{z}f''(k) = 1/\gamma - (1 - \delta). \]

Now consider the more interesting case, $\xi > 0$. It is easy to show that the planner’s optimal resource allocation satisfies

\begin{equation}
    \frac{u'(c^*_t)}{u'(c'^*_t)} < \frac{u'(c^*_t)}{u'(c'^*_t)}.
\end{equation}

Condition (15) is the restatement of a result due to Rogerson [1985]. Given the low state, individuals consume too much in the first period of their lives. If they could, they would transfer resources to the second period of their lives.

It is also easy to show that, in a steady state, a further necessary condition for optimality is

\[ \bar{z}f''(k) > 1/\gamma - (1 - \delta). \]

Hence, with private information the social planner accumulates less capital than would be accumulated under symmetric information. This result is analogous to the one reached by Khan and Ravikumar [2001]; the intuition is the same. When choosing the level of investment, the planner recognizes that a larger capital stock will make the incentive-compatibility constraint costlier to satisfy for future generations. In other words, a larger capital stock will imply less risk sharing, and thus, a lower expected marginal return. The optimal strategy is to choose a lower capital stock than would be chosen if $\xi = 0$.

In the standard two-period OLG model, the competitive equilibrium allocation may not correspond to the planner’s allocation. It is well-known, however, that there exists a simple market mechanism that results in consumption being allocated intertemporally according to (14). Does such a mechanism exist in our
more general model? For $\xi = 0$, it exists, and it is very simple. It involves introducing intermediaries that borrow from the old and lend to the young via a contract that offers full insurance to entrepreneurs. When $\xi > 0$, the answer is less obvious. It is clear, however, that such a mechanism would have to satisfy condition (15). If individuals can commit to interact with only one intermediary during their lifetime, then it is easy to prove that (15) holds. If individuals cannot commit to exclusive lifetime contracts, then the allocation will satisfy (15) only if financial institutions can perfectly monitor the agents’ use of alternative borrowing and lending opportunities. In fact, consider the case studied by Allen [1985], in which individuals can engage in unmonitored intertemporal borrowing and lending at a given interest rate. After receiving the first-period allocations from their intermediaries, individuals will trade until their consumption allocations satisfy

$$
\frac{u'(c_{1,t}^x)}{u'(c_{1,t+1}^x)} = \frac{u'(c_{h,t}^y)}{u'(c_{h,t+1}^y)}.
$$

Thus, with unmonitored borrowing and lending, any two-period contract collapses to a sequence of one-period contracts of the type considered in the main body of the paper.

APPENDIX 2: DERIVATION OF THE OPTIMAL CONTRACTING PROBLEM (P2)

In this section we cast the relationship between lender and entrepreneur as a message game with asymmetric information. Instead of surrendering their output and receiving a transfer in return, entrepreneurs simply pay a contingent return on the capital borrowed. We show that the Constrained-Pareto Optimal Contract in this environment implies the same allocation that solves problem (P1).

Differently from what is standard in the message game literature and similarly to Lacker and Weinberg [1989], we assume that besides sending a message drawn from an arbitrary space $\mathcal{M}$, each entrepreneur takes an action that consists in showing (displaying) his output to the lender. A contract at time $t$ is now given by a scalar $k_t$ and by a return function $R_t : \mathcal{M} \times [z_h,z_l] \rightarrow \mathcal{R}$. The crucial assumption is that hiding, i.e., displaying an
amount of output lower than the outcome of production, is costly.\footnote{We assume that an entrepreneur cannot display more output than he actually obtained. It is easy to prove that this assumption implies no loss of generality. That is, our results would not change if, consistently with a different notion of display, the entrepreneur could show more output than he has. This would be the case if displaying output meant disclosing balance sheet or income statement data or both.}

By the Revelation Principle, we can restrict our attention to the case in which \(\mathcal{M} = \{z_h, z_l\}\) and the reports are truthful. However, we do not require the amounts displayed to be consistent with the reports. After having observed his outcome \(z_t f(k_t)\), the entrepreneur makes a claim about the quality of his project \(\hat{z}_t \in \{z_h, z_l\}\) and displays output in measure \(\tilde{z}_t\). Feasibility requires that \(\tilde{z}_t = z_t\) and \(z_h \in \{z_h, z_l\}\). Finally, he transfers to the lender an amount \(R_t(\hat{z}, \tilde{z}) k_t\).

A contract at time \(t\) is a capital advance \(k_t\) and a return schedule \(R_t(\hat{z}, \tilde{z})\) that solve

\[
\max_{k_t, \hat{z}_t \in \{z_h, z_l\}, R(\hat{z}, \tilde{z})} \rho v[zh f(k_t) - R_t(z_h, \tilde{z})k_t - (1 - \xi)(z_h - \tilde{z}) f(k_t), r_{t+1}]
+ (1 - \rho) v[z_t f(k_t) - R_t(z_l, z_l)k_t, r_{t+1}],
\]

subject to

\[
\rho R_t(z_h, \tilde{z}_h) + (1 - \rho) R_t(z_l, z_l) = r_t + \delta
\]

(16) \((z_h, \tilde{z}_h) = \arg \max_{\hat{z}, \tilde{z} \in \{z_h, z_l\}} v[zh f(k_t) - R_t(z_h, \tilde{z})k_t - (1 - \xi)(z_h - \tilde{z}) f(k_t), r_{t+1}]
+j = \arg \max_{\hat{z}, \tilde{z} \in \{z_h, z_l\}} v[z_t f(k_t) - R_t(z_l, z_l)k_t, r_{t+1}].
\]

The deadweight loss associated with hiding cash flows in the high state is \((1 - \xi) \Delta f(k_t)\), i.e., a fraction \((1 - \xi)\) of the output hidden. Condition (16) requires truthful reporting and optimal display of output by high-outcome entrepreneurs. Condition (17) requires truthful reporting by low-outcome entrepreneurs. Following an argument made by Lacker and Weinberg [1989], Lemma 1 shows that the optimal return schedule is independent of the report \(\tilde{z}\).

**LEMMA 1.** For all \(\tilde{z} \in \{z_h, z_l\}\), \(R_t(z_h, \tilde{z}) = R_t(z_l, \tilde{z})\) without loss of generality.

**Proof of Lemma 1.** We first show that \(R_t(z_h, z_l) = R_t(z_l, z_l)\). Condition (17) implies that \(R_t(z_h, z_l) \geq R_t(z_l, z_l)\). If \(\tilde{z}_h = z_l\), then

\[
R_t(z_h, z_l) \geq R_t(z_l, z_l).
\]
(16) implies that \(-R_t(z_h,z_l)k_t - (1 - \xi)\Delta f(k_t) \geq -R_t(z_l,z_l)k_t - (1 - \xi)\Delta f(k_t)\). In turn, this implies that \(R_t(z_h,z_l) \leq R_t(z_l,z_l)\). Instead, if \(\tilde{z}_h = z_h\), then it must be the case that \(-R_t(z_h,z_h)k_t \geq -R_t(z_l,z_l)k_t - (1 - \xi)\Delta f(k_t)\). Since \(R_t(z_h,z_l)\) does not appear anywhere else in the problem, there is no loss in generality in imposing \(R_t(z_h,z_l) = R_t(z_l,z_l)\).

We now show that \(R_t(z_h,z_h) = R_t(z_l,z_h)\). If \(\tilde{z}_h = z_h\), then (16) implies that \(R_t(z_l,z_h) \geq R_t(z_l,z_h)\). Instead, if \(\tilde{z}_h = z_l\), then (16) implies that \(-R_t(z_h,z_l)k_t - (1 - \xi)\Delta f(k_t) \geq -R_t(z_l,z_l)k_t\). In either case, \(R_t(z_h,z_h)\) does not appear anywhere else in the problem. Therefore, there is no loss in generality in imposing that \(R_t(z_l,z_h) = R_t(z_h,z_h)\).

In light of Lemma 1, we can rewrite the optimal contracting problems as

\[
\max_{k_t, \tilde{z} \in \{z_h,z_l\}, R_t(\tilde{z})} \rho v[z_t f(k_t) - R_t(\tilde{z})k_t]
\]

\[-(1 - \xi)(z_h - \tilde{z})f(k_t) + (1 - \rho)v[z_t f(k_t) - R_t(z_l)k_t, r_{t+1}],\]

subject to

\[
(18) \quad \rho R_t(\tilde{z}_h) + (1 - \rho)R_t(z_l) = r_t + \delta
\]

\[
\tilde{z}_h = \arg \max_{\tilde{z} \in \{z_h,z_l\}} v[z_h f(k_t) - R_t(\tilde{z})k_t - (1 - \xi)(z_h - \tilde{z})f(k_t), r_{t+1}].
\]

Lemma 2 shows that no Constrained-Pareto Optimal contracts involve hiding.

**Lemma 2.** Hiding is never optimal; i.e., \(\tilde{z}_h = z_h\).

**Proof of Lemma 2.** By contradiction, assume that the optimal contract \(\{k_t, R_t(\cdot)\}\) implies that \(\tilde{z}_h = z_l\). Consider the return schedule \(R'_t(\cdot)\) such that \(R'_t(z_h) = R'_t(z_l) = R_t(z_l)\). The contract \(\{k_t, R'_t(\cdot)\}\) implies that \(\tilde{z}_h = z_h\), satisfies (18), and provides the entrepreneur with a strictly greater utility. This contradicts the initial assumption.

The intuition for this result is simple. The spread between the incomes of high- and low-outcome entrepreneurs is invariant to the level of output displayed \(\tilde{z} f(k_t)\). In any contract that prescribed hiding, the income of high-outcome entrepreneurs is given by \(z_h f(k_t) - R_t(z_l)k_t - (1 - \xi)\Delta f(k_t)\). Therefore, \(m_t(z_h) -
Since \( v(\cdot, r_t) \) is strictly increasing and strictly concave, any optimal contract with no hiding will require 
\[ R_t(z_h) = R_t(z_i) - (1 - \xi)\Delta f(k_t). \]
Thus, also in this case, 
\[ m_i(z_h) - m_i(z_i) = \xi \Delta f(k_t). \]
In the case of no hiding, however, the total surplus is larger, as there is no deadweight loss. \(^{36}\)

Lemma 2 also holds in the case in which a portion of \((1 - \xi)\Delta f(k_t)\) accrues to the intermediary. In the extreme case in which there is no deadweight loss, optimal contracts with hiding and no hiding imply the same allocation. \(^{37}\)

By Lemma 2 we can now restate the optimal contracting problem as follows:

\[
\begin{align*}
(P2) \quad \max_{k_t, R_t(z_h), R_t(z_i)} & \quad \rho v[z_hf(k_t) - R_t(z_h)k_t, r_{t+1}] \\
& \quad + (1 - \rho)v[z_if(k_t) - R_t(z_i)k_t, r_{t+1}],
\end{align*}
\]

subject to

\[
\rho R_t(z_h) + (1 - \rho)R_t(z_i) = r_t + \delta
\]

\[
v[z_hf(k_t) - R_t(z_h)k_t, r_{t+1}] \\
\geq v[z_if(k_t) - R_t(z_i)k_t - (1 - \xi)\Delta f(k_t), r_{t+1}].
\]

It is now evident that for any contract \( \{k_t, R_t(z_h), R_t(z_i)\} \) that solves problem (P2), there is a contract \( \{k_t, \tau_t(z_h), \tau_t(z_i)\} \) with \( \tau(z_i) \equiv z_if(k_t) - R_t(z_i)k_t \) for \( i = h, l \)

that solves Problem (P1) and implies the same levels of income \( m_i(z_h) \) and \( m_i(z_i) \).

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\(^{36}\) Lacker and Weinberg [1989] also note that when the hiding cost function is linear, then contracts with no hiding are always optimal. However, the same authors show the existence of alternative specifications of the cost function for which Lemma 2 does not hold.

\(^{37}\) The proof of this statement is available from the authors upon request. It was not included because it requires working with a continuum of outcomes. In fact, with a discrete set of outcomes, any hiding would be detected by the lender.


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